

Minimal Design for Decentralized Wallet

Omer
Shlomovits



Motivation

* Imagine we had a private key management system where:

- ▶ *No single point of failure*
- ▶ *Move of assets (signing) cannot happen without Owner approval*
- ▶ *Recovery is possible at all times*

Our Heroes

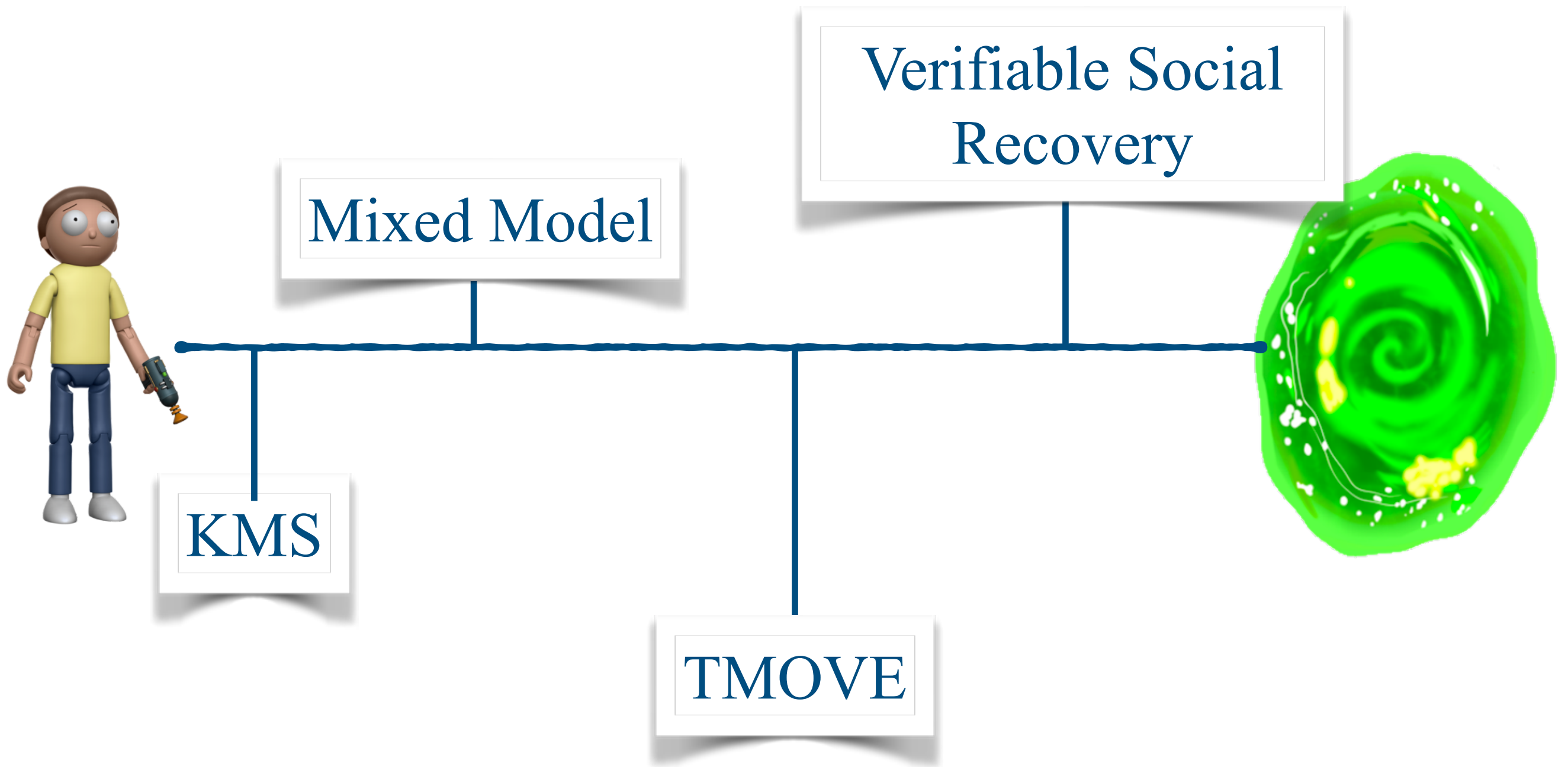


Rick



Morty

The Journey

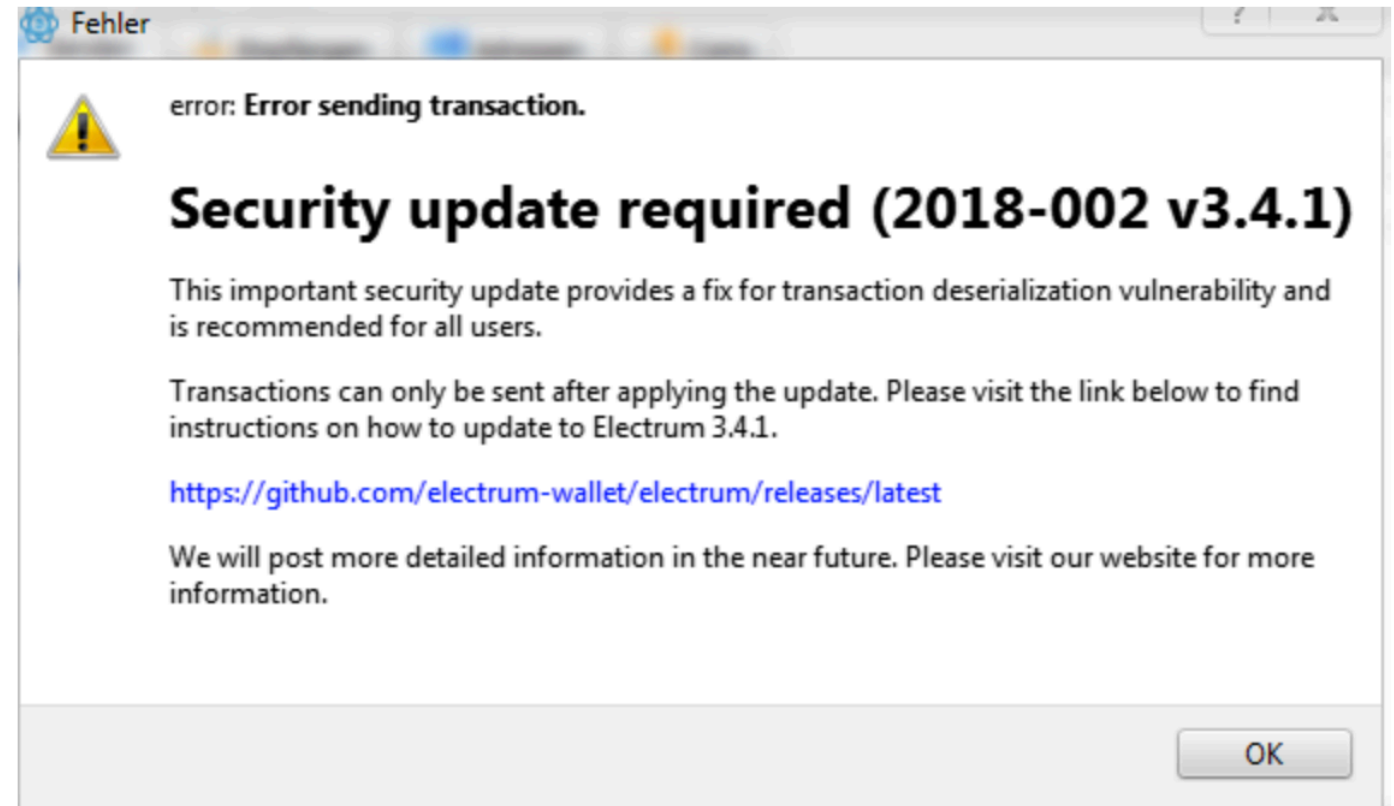


Key Management System

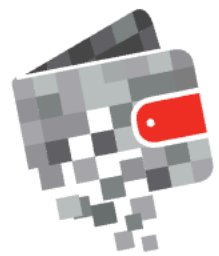
- * Three main functionalities in the context of blockchains:
 - ▶ Key generation and custody
 - ▶ Signatures
 - ▶ Key backup and recovery

⁶Problem: Key Management is hard

- * Side channel attacks
- * social engineering attacks
- * human errors
- * etc...



Fake alert created by the attacker (via Electrum GitHub page)



WALLET.FAIL

Poof goes your crypto ...



devops199 commented 22 hours ago • edited

I accidentally killed it.

<https://etherscan.io/address/0x863df6bfa4469f3ead0be8f9f2aae51c91a907b4>

Trusted Party to the rescue?

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2018: A Record-Breaking Year for **Crypto Exchange Hacks**

CoinDesk - 29 Dec 2018

From the number of **cryptocurrency exchange** hacks, to the amount of assets that were stolen, to the largest **exchange hack** of all-time, **crypto** ...



How Hackers Stole \$1B From **Cryptocurrency Exchanges** In 2018

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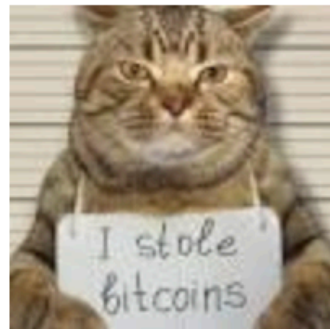
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How can we optimize on **keys security** without compromising on **keys usability** ?

From single to distributed keys

*Enter threshold cryptography

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- *Enter threshold cryptography
- *Given n parties, we divide the key management responsibilities
 - ▶ Distributed key generation
 - ▶ Signing requires cooperation of t out of n

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- *Enter threshold cryptography
- *Given n parties, we divide the key management responsibilities
 - ▶ Distributed key generation
 - ▶ Signing requires cooperation of t out of n
- *Efficient protocols exists
 - ▶ Threshold ECDSA [GG18, DKLS18, LNR18]

Sounds a lot like
Multisig to me



Multisig vs Threshold Signing

<https://medium.com/kzen-networks/threshold-signatures-private-key-the-next-generation-f27b30793b>

- *Max number of parties
- *Interactiveness
- *Rotation
- *Access policy privacy
- *Chain support
- *Low cost
- *Efficiency (communication/ computation)

Multisig vs Threshold Signing

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Mixed Model

Mixed Model

* Roles

▶ *Owner* *x 1*

▶ *Service Providers*

Mixed Model {t=n=2}

* Roles

▶ *Owner* $\times 1$

▶ *Service Providers* $\times 1$

Mixed Model {t=n=2}

* Roles

- ▶ Owner *x 1*
- ▶ Service Providers *x 1*

* System Requirements

- ☑ *No single point of failure*
- ☑ *Move of assets (signing) cannot happen without Owner approval*
- ▶ *Recovery is possible at all times ?*

Choosing Parameters $\{t,n\}$

- * Depends on the adversary model and specific use case different access structures can be considered
- * Axiom: assuming SP is motivated solely by Economical Gain, We cannot avoid the Recovery problem
- * Fact: two-party protocols are simpler than multi-party protocols

Recovery in Mixed Model {t=n=2}

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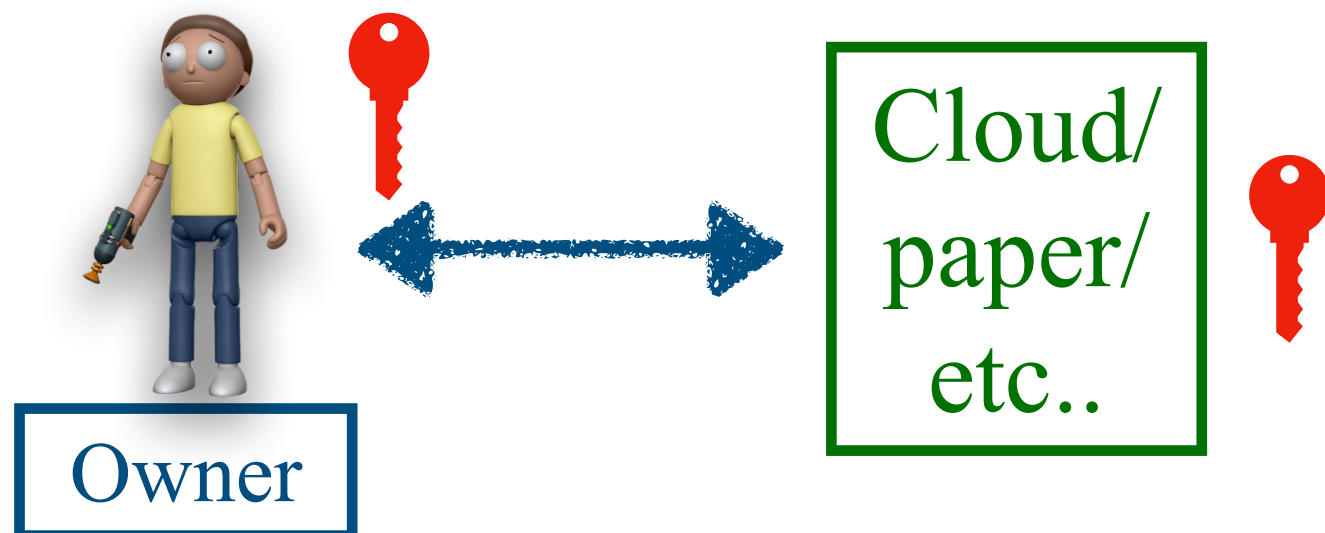
*Recovery in the two party setting can mean:

- Self recovery: Owner's secret share
- Counter party recovery: SP secret share



Recovery in Mixed Model {t=n=2}

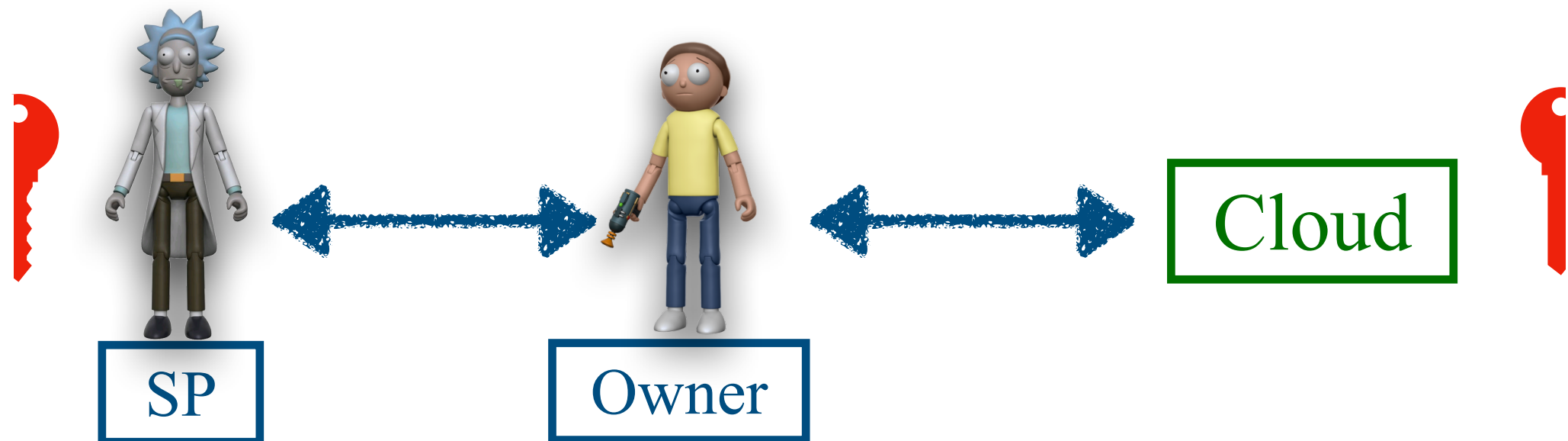
*Owner self-recovery reduces to classical backup



Recovery in Mixed Model {t=n=2}

*Owner self-recovery reduces to classical backup

► Assuming Authentication:



Recovery in Mixed Model $\{t=n=2\}$

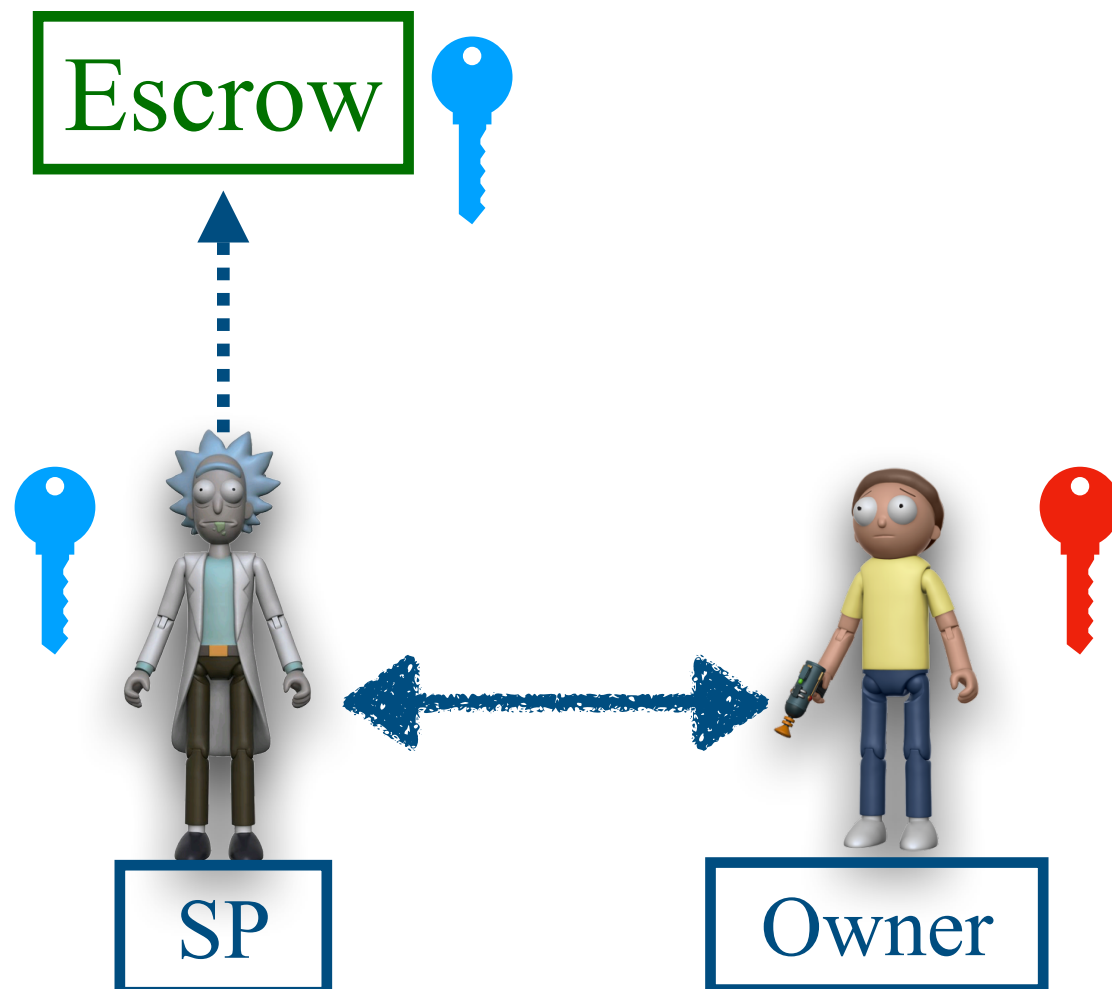
*Recovery in the two party setting can mean:

- ▶ Self recovery: Owner's secret share
- ▶ **Counter party recovery: SP secret share**
 - How can the Owner recover if SP goes offline / hacked / becomes malicious ?



Recovery of Counter Party Secret

- * How can we recover Counter secret share if SP goes offline / hacked / becomes malicious ?
- * Under certain assumptions this can be done easily.
 - Escrow service that is triggered to release SP secret share once SP is not sending a life signal for a certain period of time

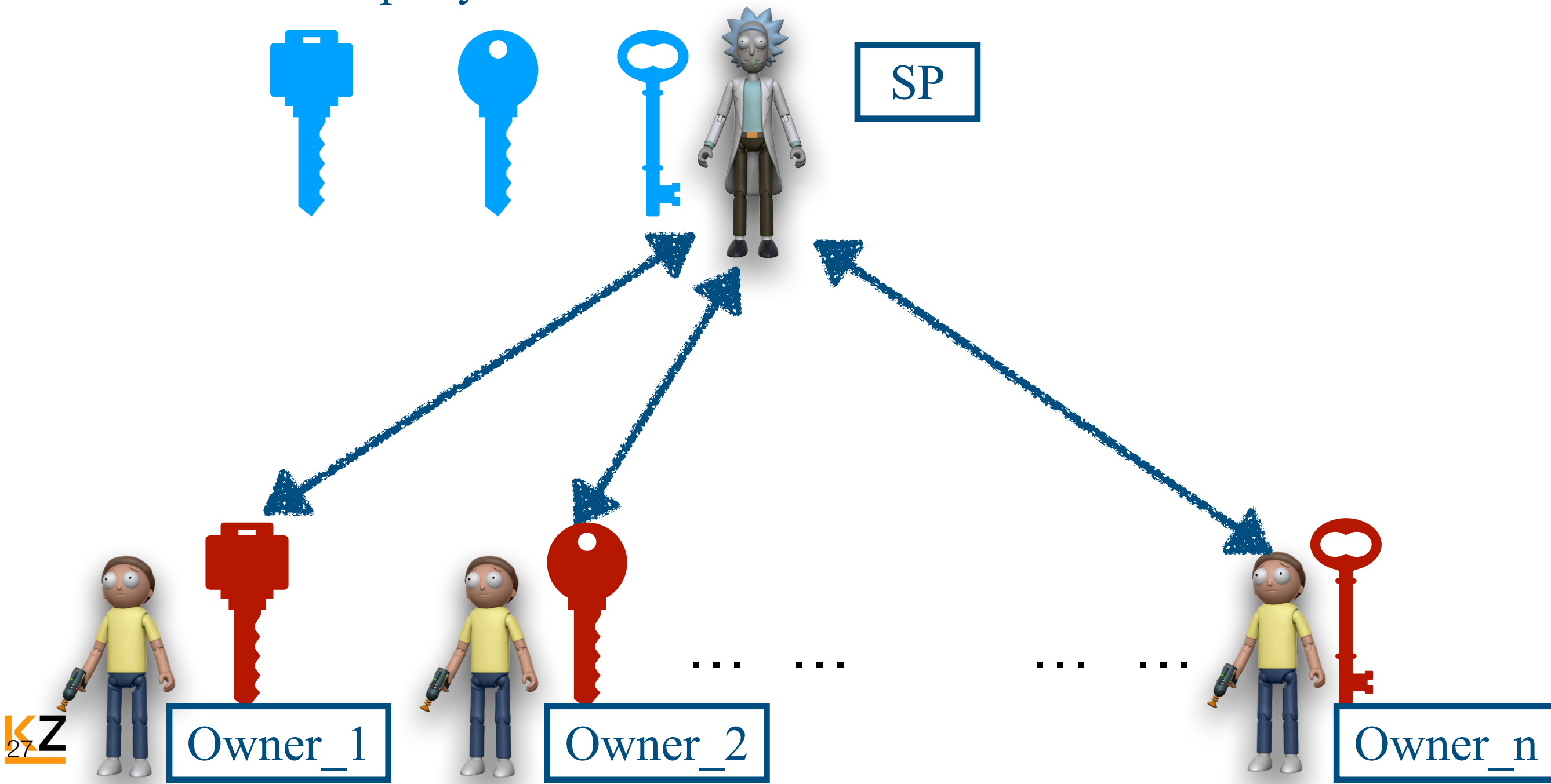


$$sk = f(\text{red key}, \text{blue key})$$

Recovery of Counter Party Secret

* general idea:

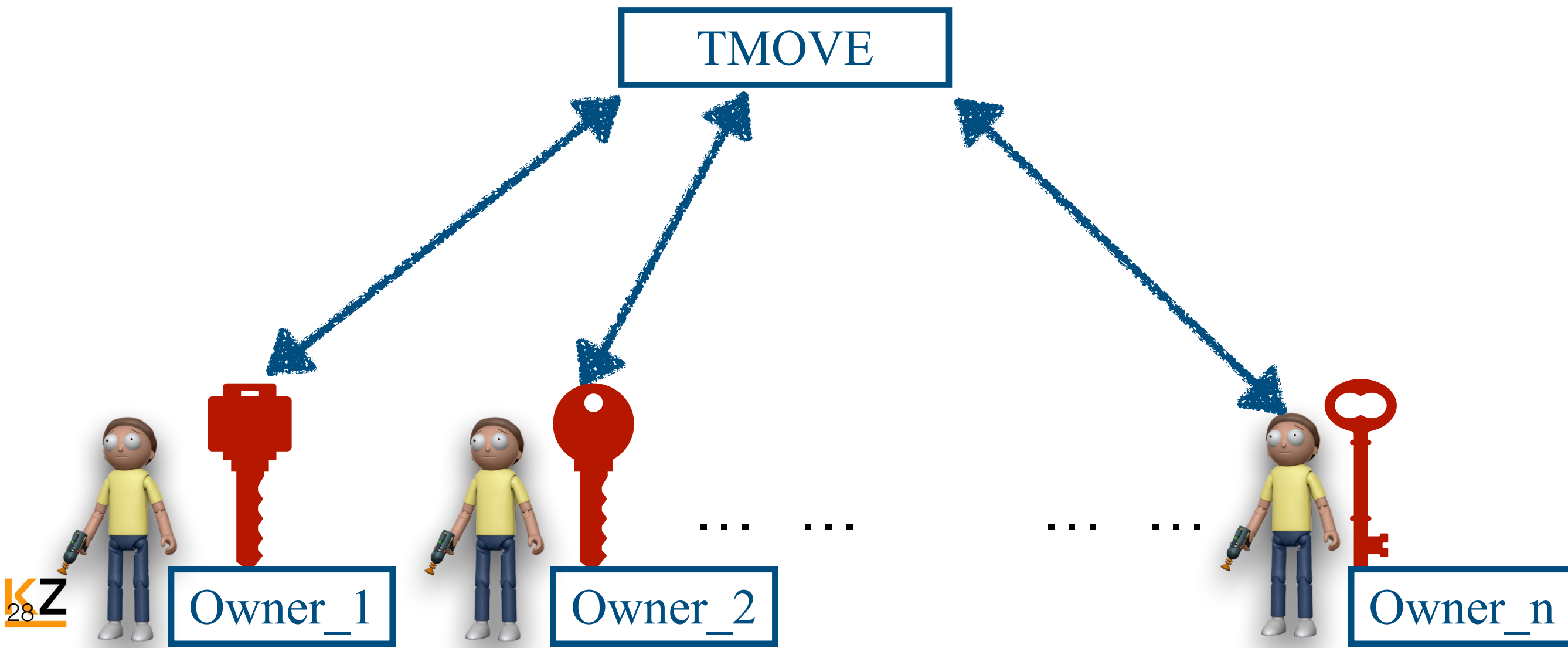
- If enough Owners collaborate, they each get to recover their Counter party secret share at the same time



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Background: PVSS [S99]

Publicly Verifiable Secret Sharing

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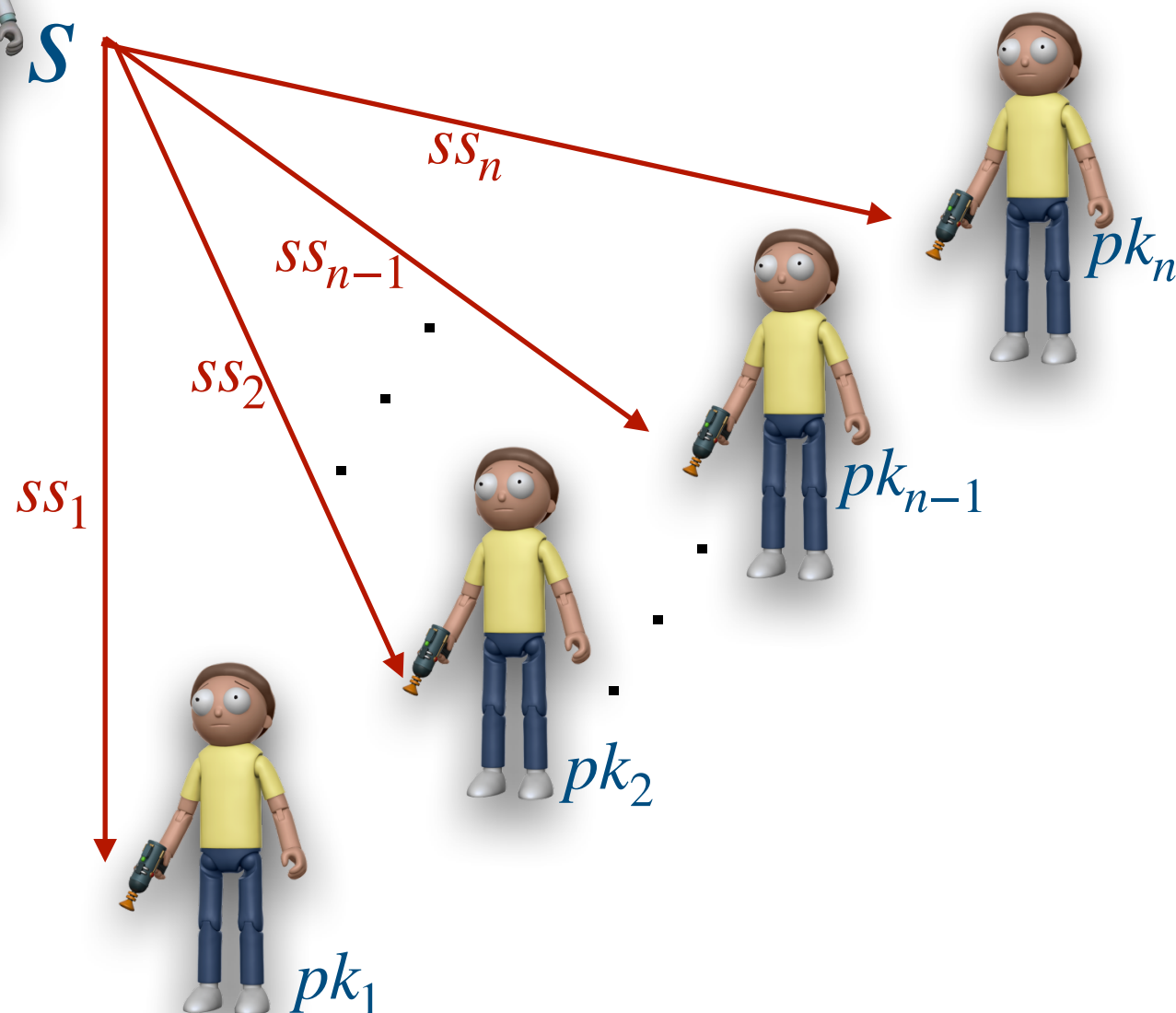
Publicly Verifiable Secret Sharing

Dealer



S

Distribution



Background: PVSS

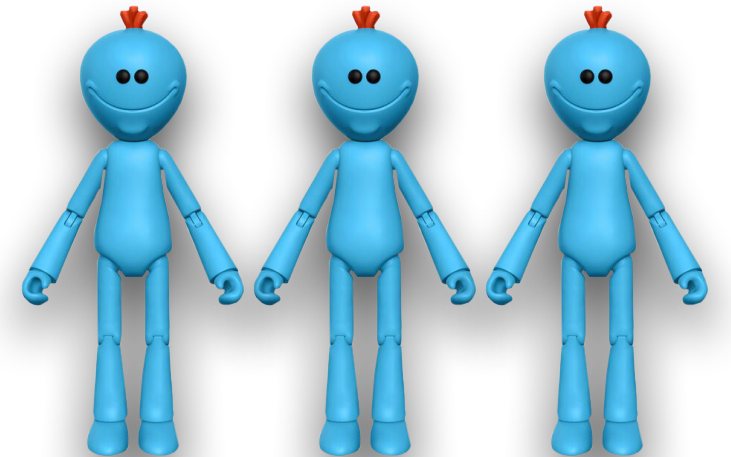
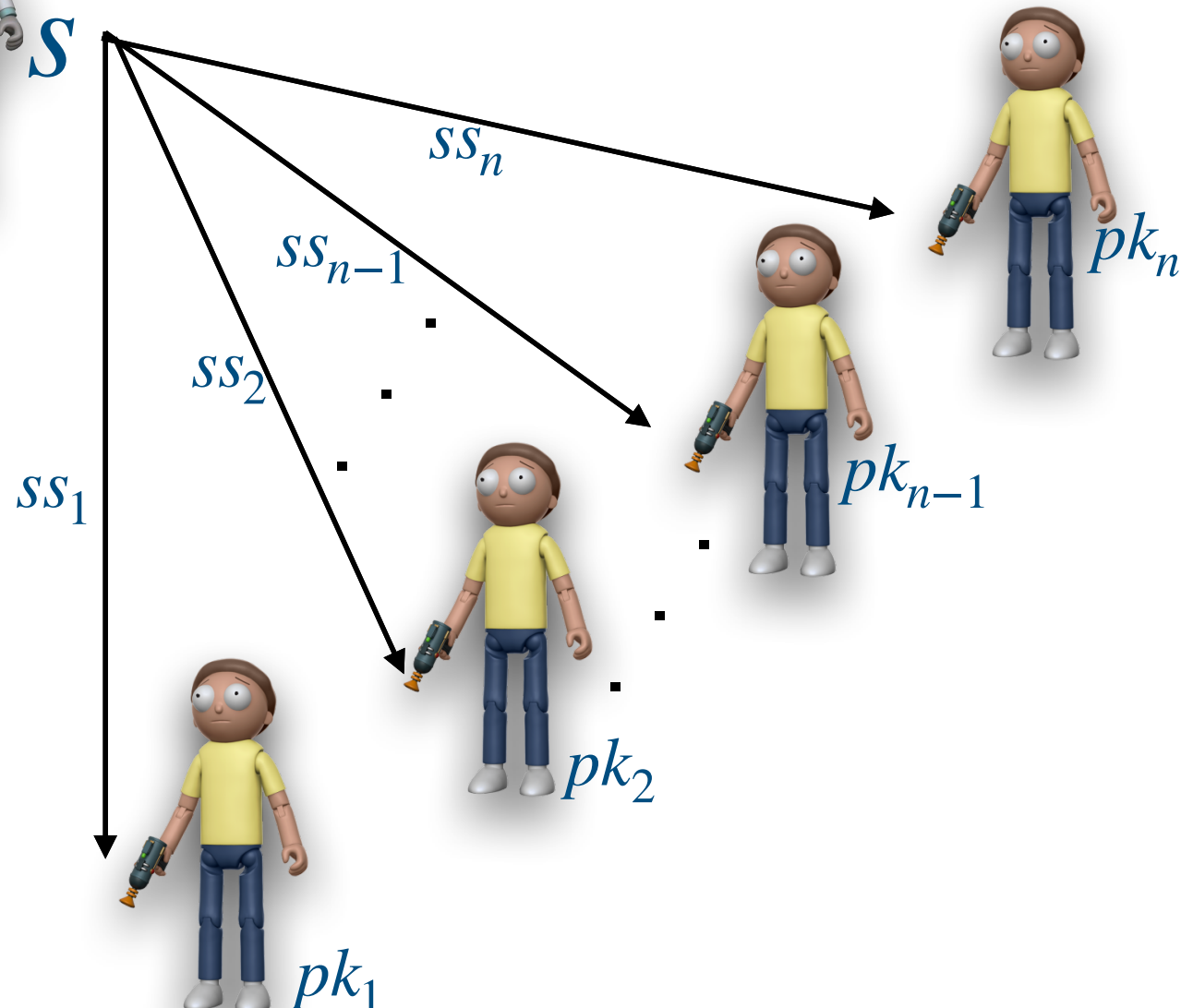
Publicly Verifiable Secret Sharing

public proofs : A dealer cannot send incorrect shares

Dealer



S

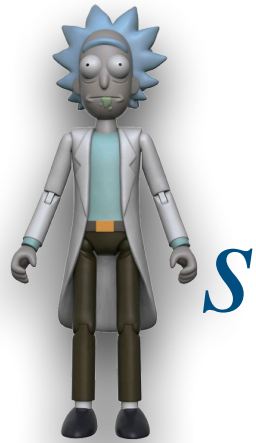


$\{\pi_{d_i}\}_1^n$

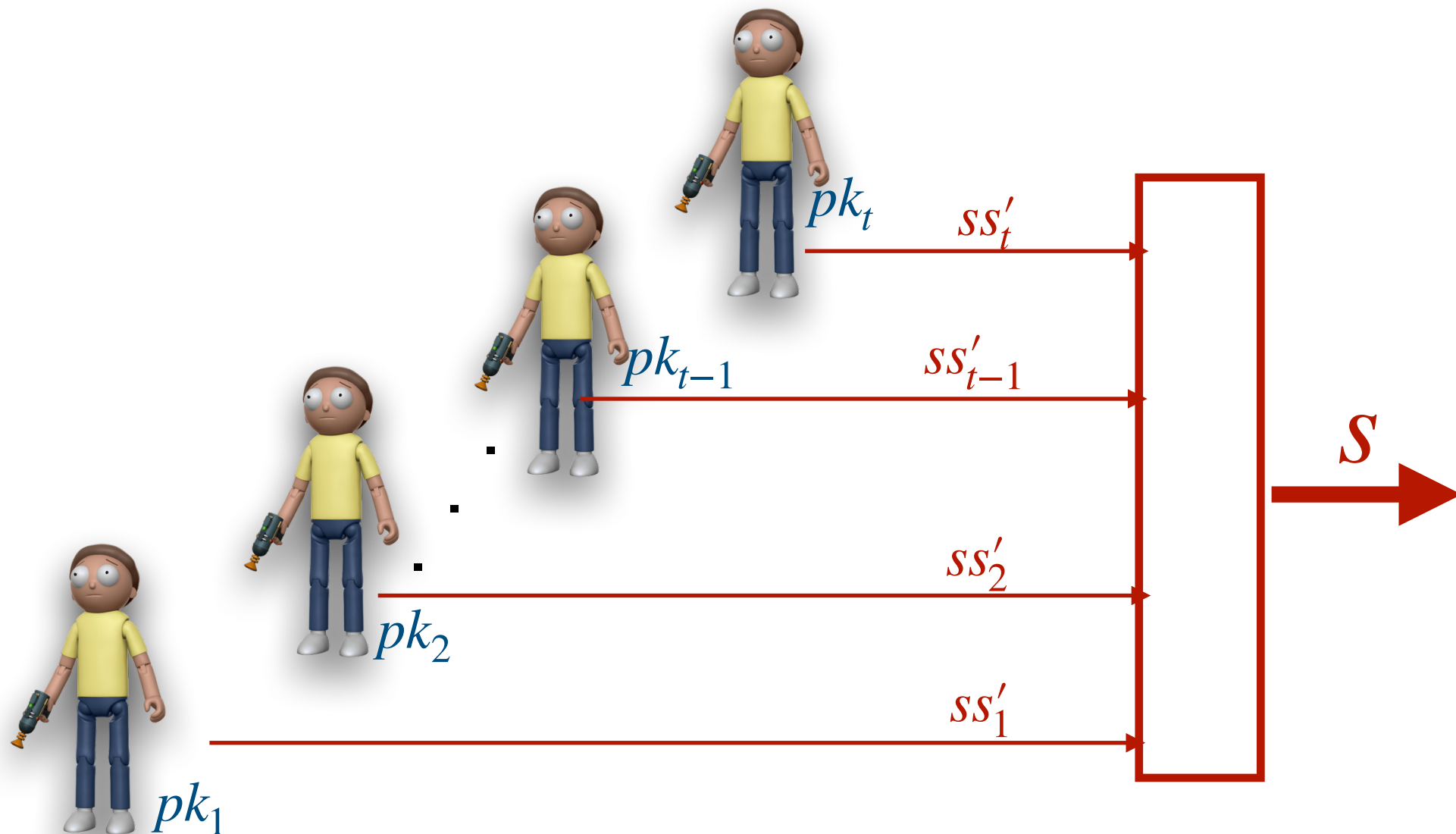
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Dealer



Reconstruction: t out of n

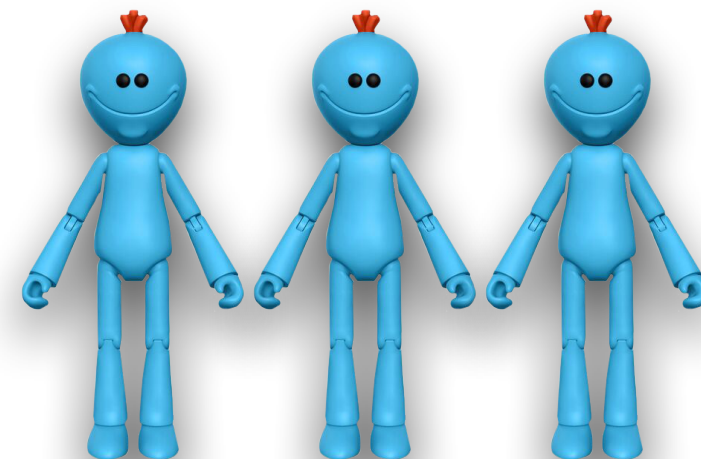


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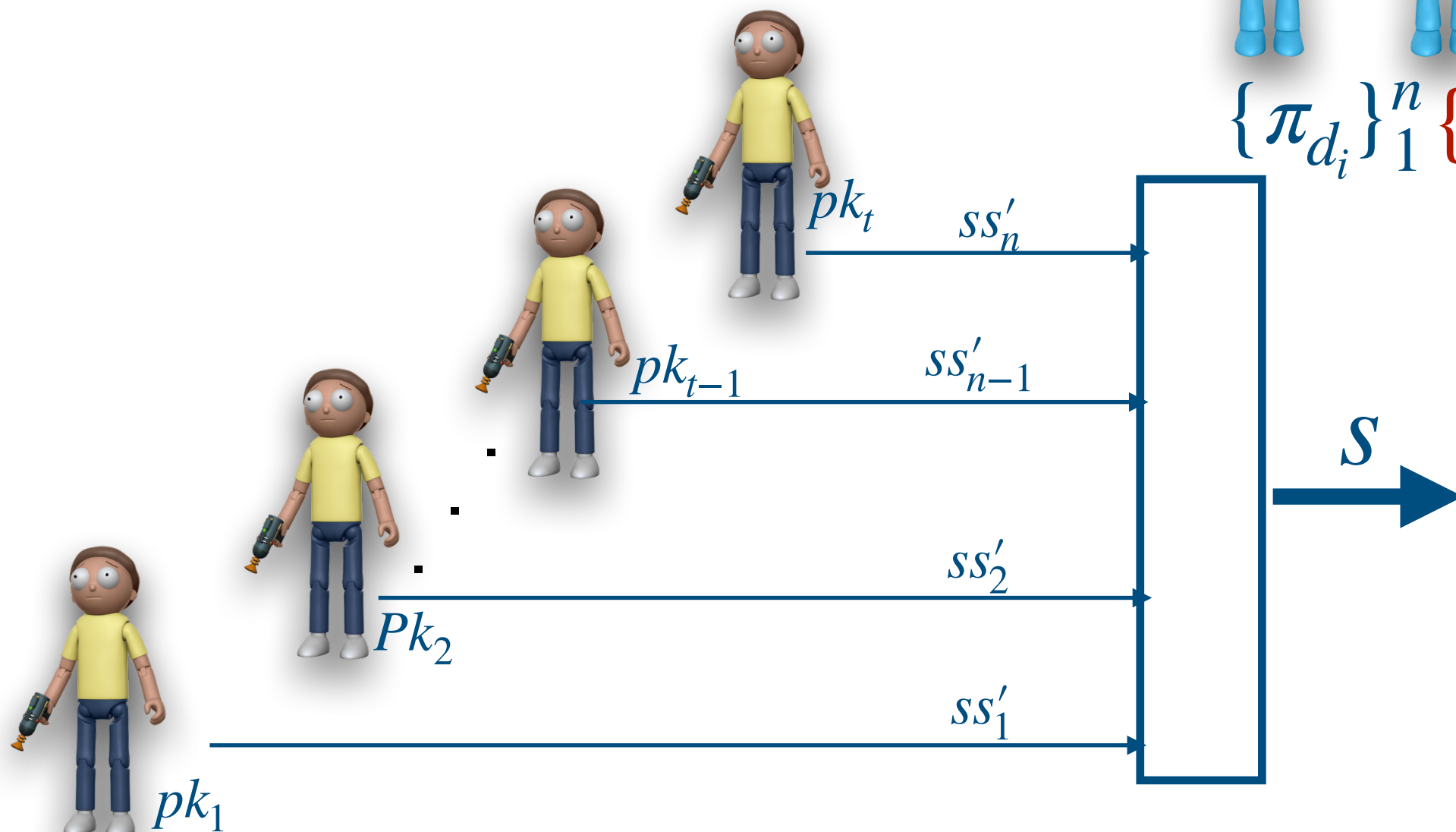
Publicly Verifiable Secret Sharing

Public proofs: Participants cannot submit incorrect shares

Dealer



$$\{\pi_{d_i}\}_1^n \{\pi_{r_i}\}_1^t$$



Background: DLog VE [CS03]

Verifiable Encryption of Discrete Log

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Verifiable Encryption of Discrete Log

$$\{Gen, Enc, Dec\}$$

$$\{x, \omega\} \in R_{dlog}$$



$$\{sk_m, pk_m\} \leftarrow Gen(1^n)$$

Background: DLog VE [CS03]

Verifiable Encryption of Discrete Log



$$c, \pi \leftarrow \text{Enc}^\star(\omega, pk_m)$$

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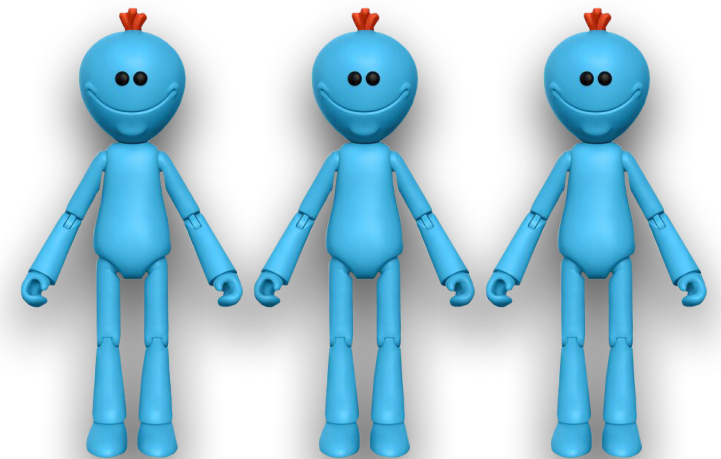
Verifiable Encryption of Discrete Log



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$$1/0 \leftarrow V(c, \pi, x, pk_m)$$



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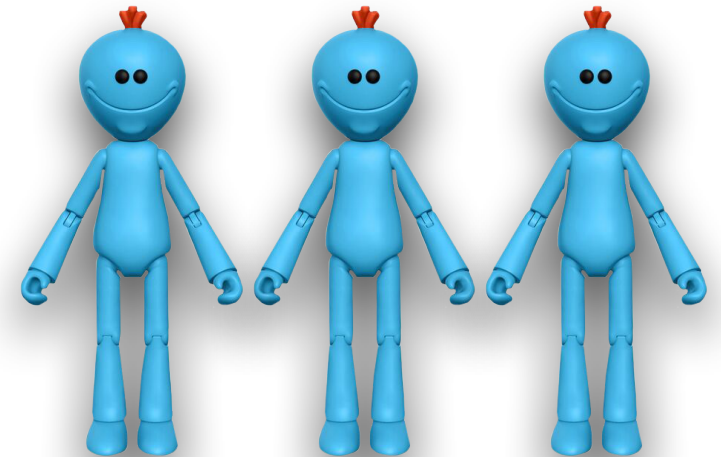
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$$\omega \leftarrow \text{Dec}^*(c, sk_m)$$

TVE

Threshold Verifiable Encryption

TVE

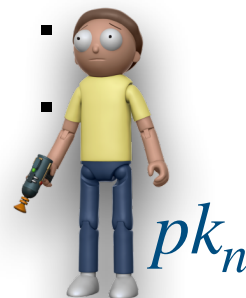
Threshold Verifiable Encryption

$\{Gen, Enc, Dec\}$

$\{x, \omega\} \in R_{dlog}$



•



$\{sk_m, pk_m\} \leftarrow Gen(1^n)$

TVE

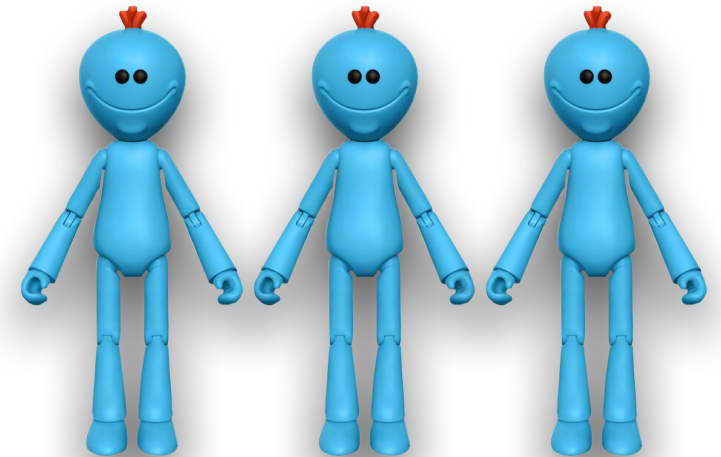
Threshold Verifiable Encryption



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⋮



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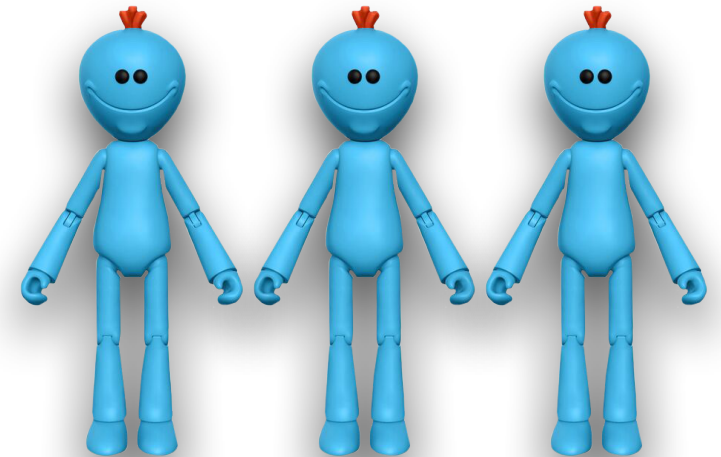


$$c, \pi \leftarrow \text{Enc}^*(\omega, \{pk_i\}_1^n, pk_m)$$

PVSS::distribute

$$\{Gen, Enc, Dec\}$$

$$\{x, \omega\} \in R_{dlog}$$



$$1/0 \leftarrow V(c, \pi, x, pk_m)$$

$$\{\pi_{d_i}\}_1^n$$



•



$$\{sk_m, pk_m\} \leftarrow Gen(1^n)$$

TVE

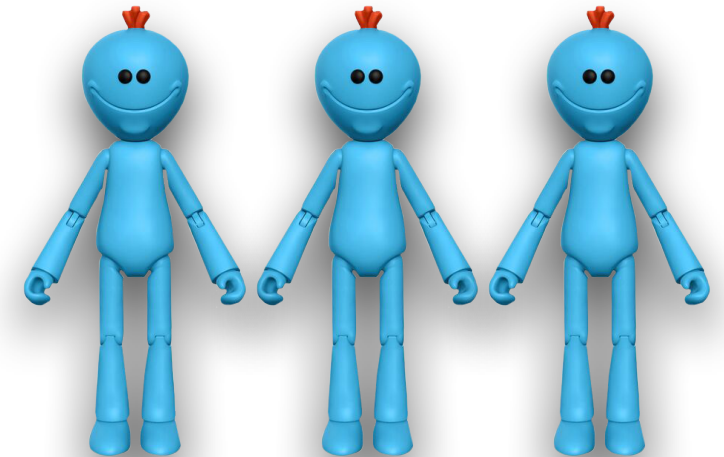
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$$1/0 \leftarrow V(c, \pi, x, pk_m)$$

$$\{\pi_{d_i}\}_1^n \quad \{\pi_{r_i}\}_1^t$$



•



PVSS::reconstruct



$$\{sk_m, pk_m\} \leftarrow Gen(1^n)$$

TVE

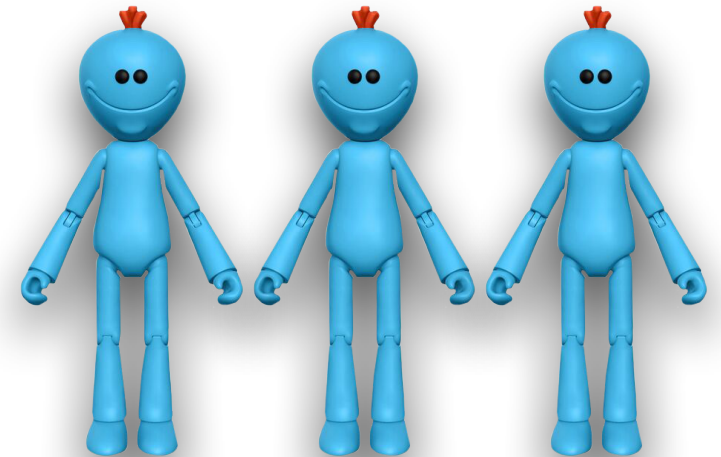
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$$1/0 \leftarrow V(c, \pi, x, pk_m) \\ \{\pi_{d_i}\}_1^n \{\pi_{r_i}\}_1^t$$



•



$$\omega \leftarrow \text{Dec}^*(c, sk_m, \{ss_i\}_1^t, Dec)$$



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TMOVE

Threshold Multiple Output Verifiable Encryption

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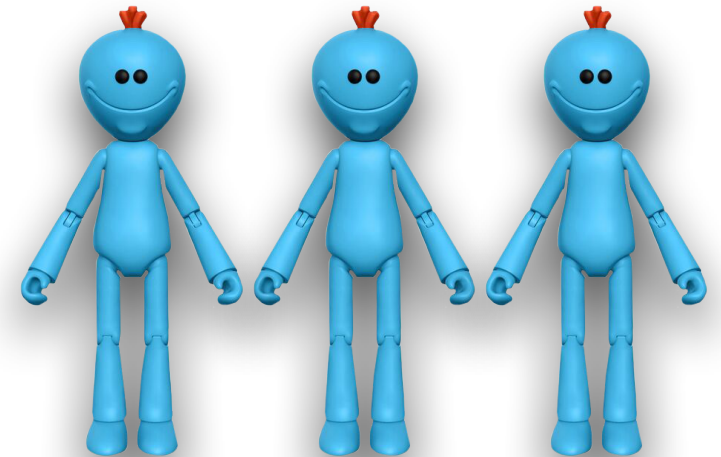
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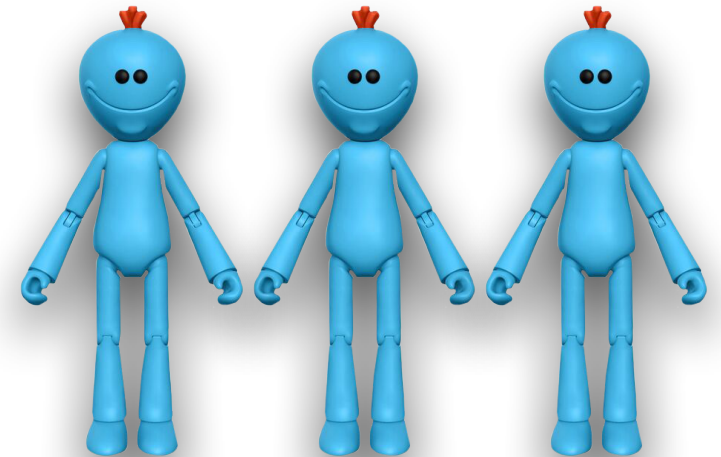

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 $\{c_i\}_1^n, \pi \leftarrow Enc^*(\{\omega_i\}_1^n, \{pk_i\}_1^n)$
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 $\{ \{ \pi_{d_{ij}} \}_{i=1}^n \}_{j=1}^m$

PVSS::distribute

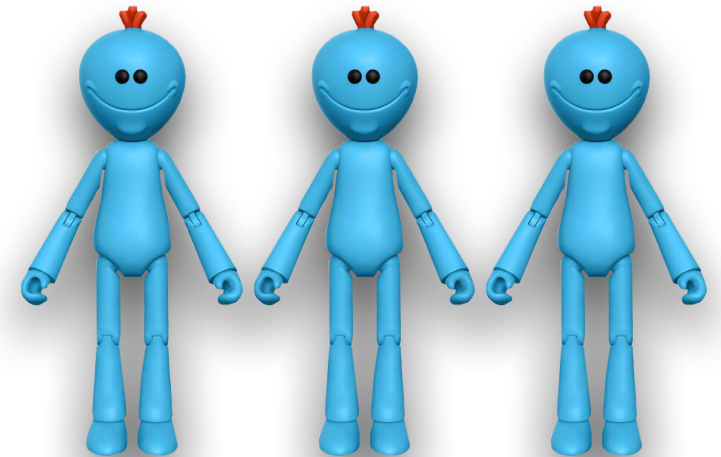


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$$\left\{ \left\{ \pi_{d_{ij}} \right\}_{i=1}^n \right\}_{j=1}^m$$

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PVSS::reconstruct

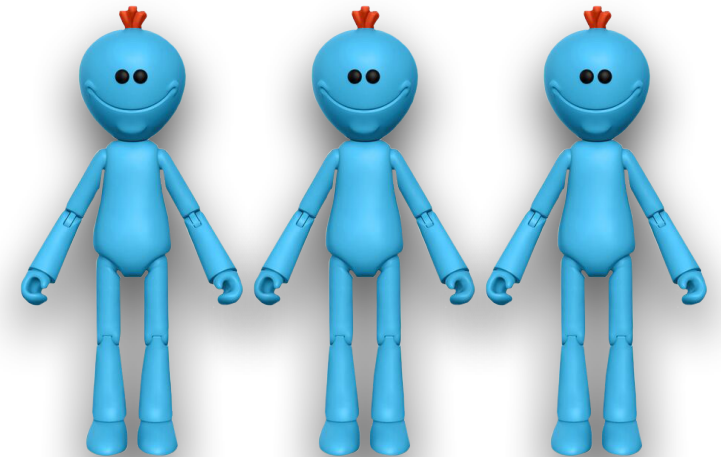
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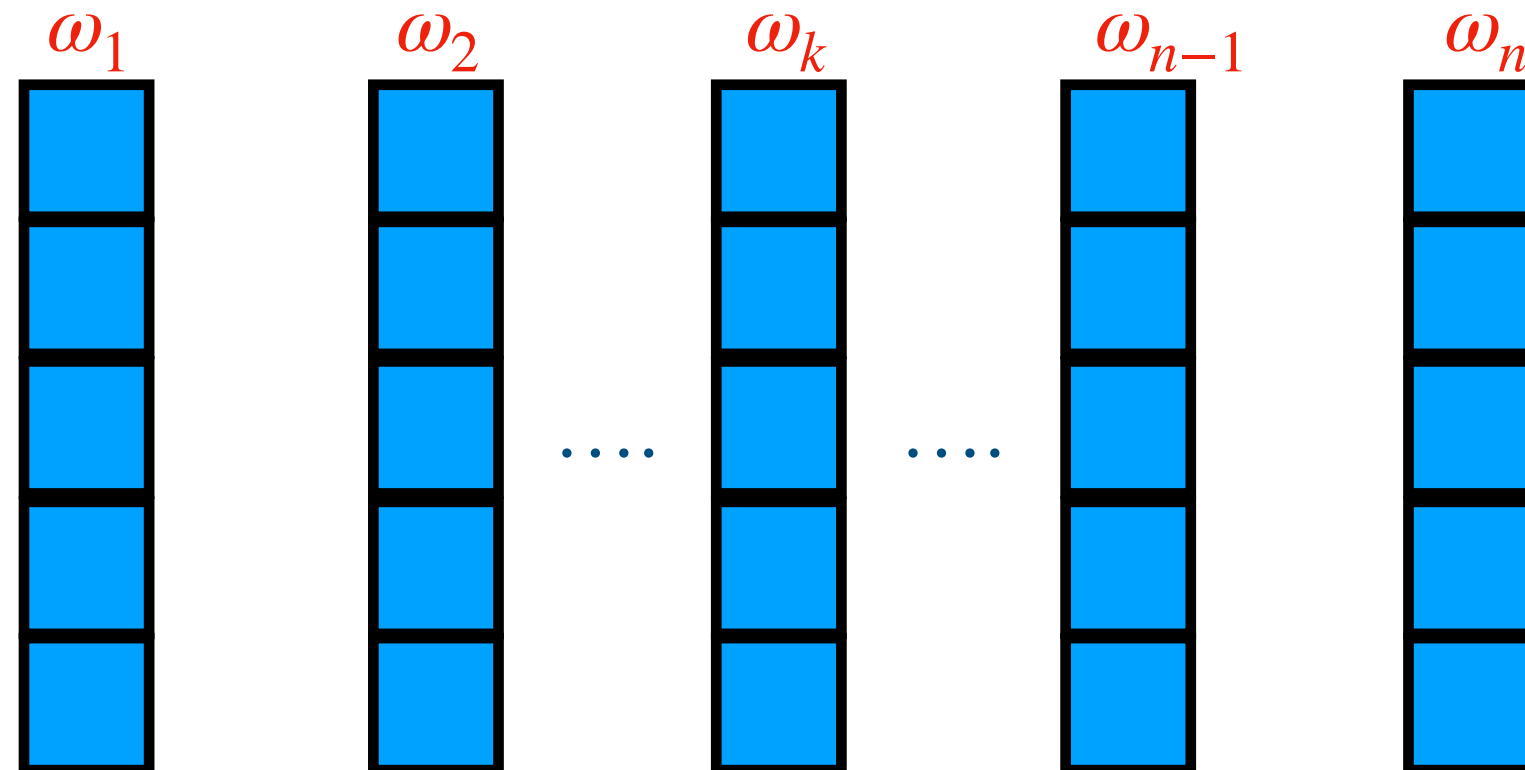


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$\omega_k \leftarrow Dec^*(c_k, sk_k, \left\{ \left\{ ss_i \right\}_{i=1}^{t_j} \right\}_{j=1}^m)$

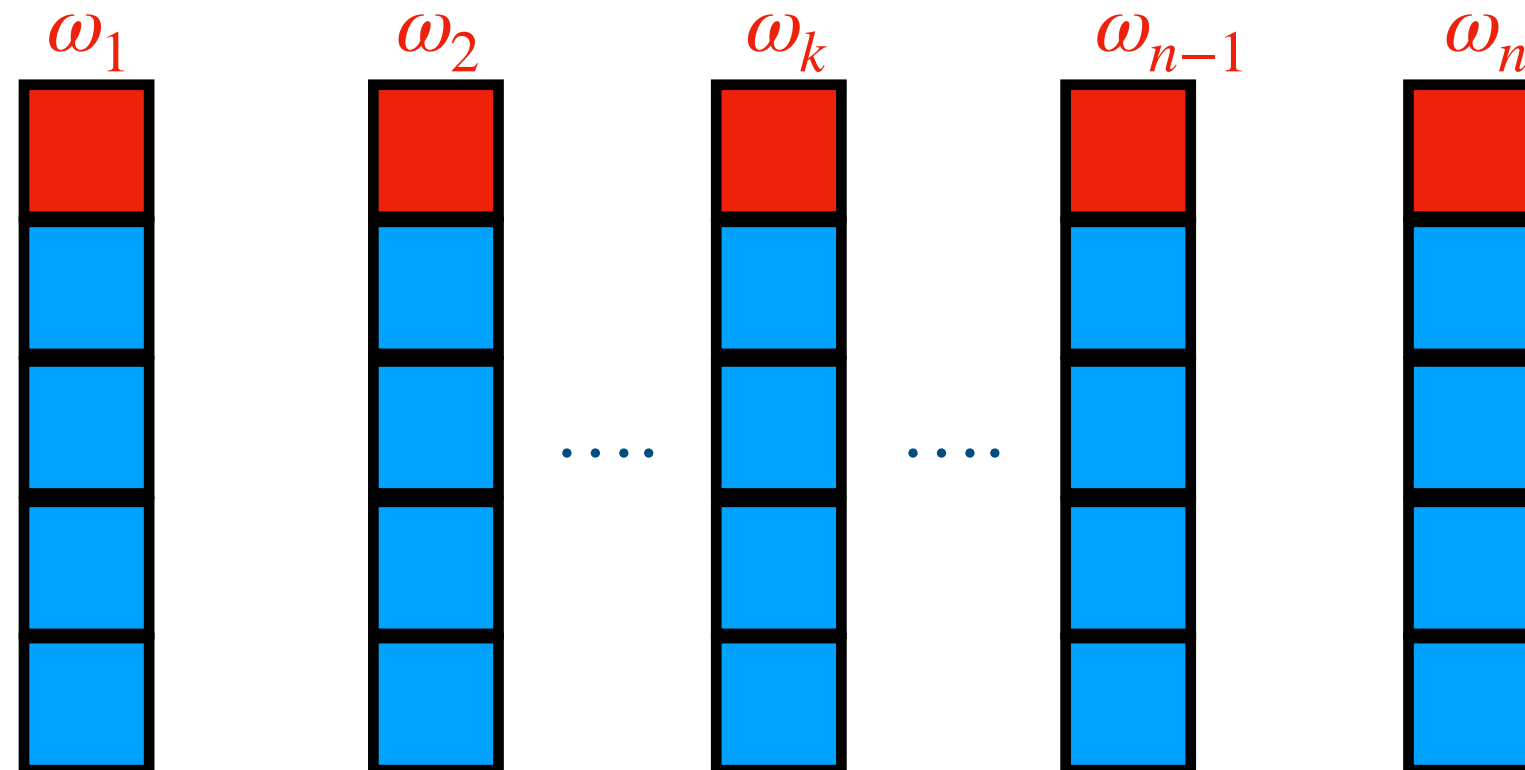
TMOVE Properties

- * TVE per party
- * Gradual release (up to one segment)



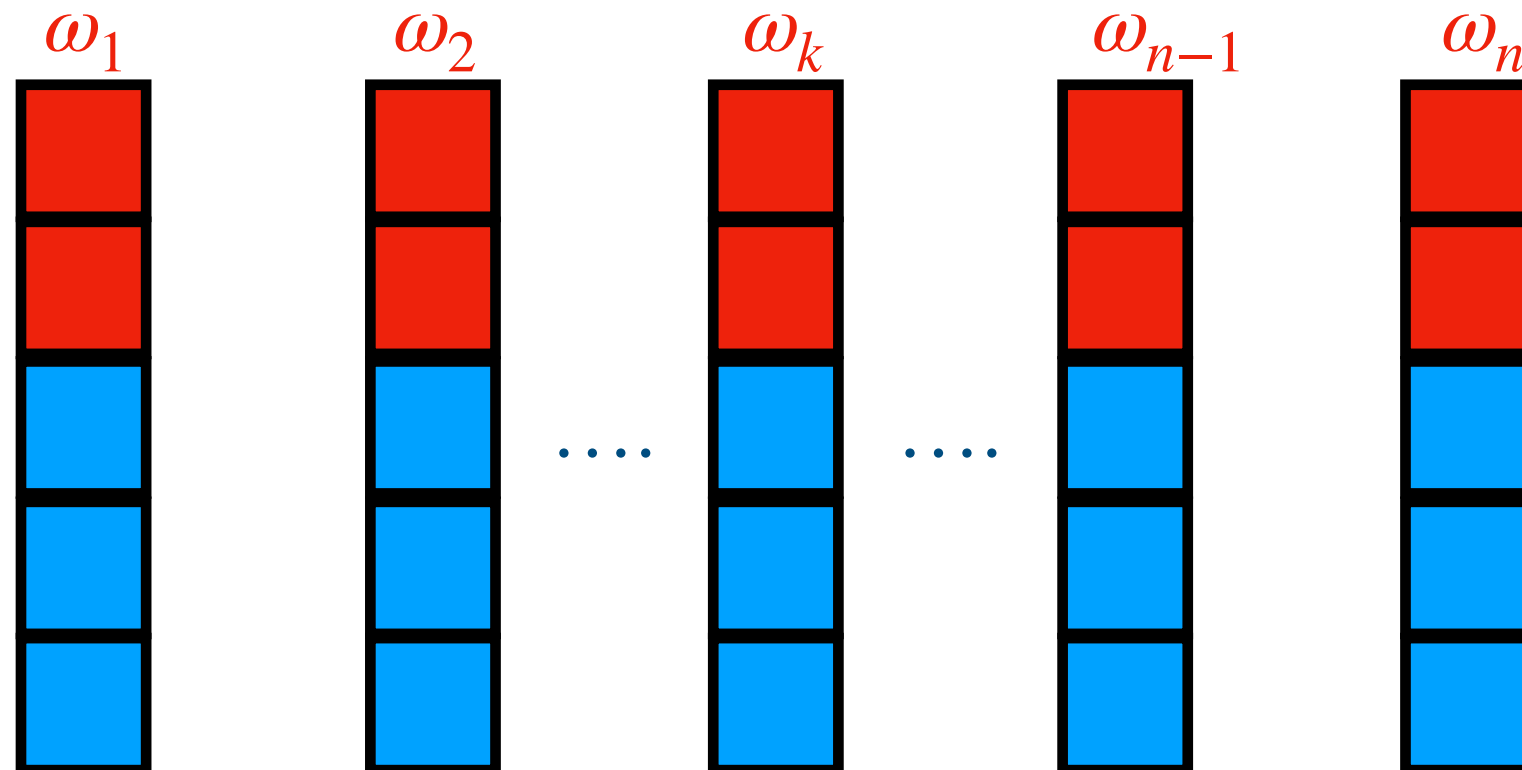
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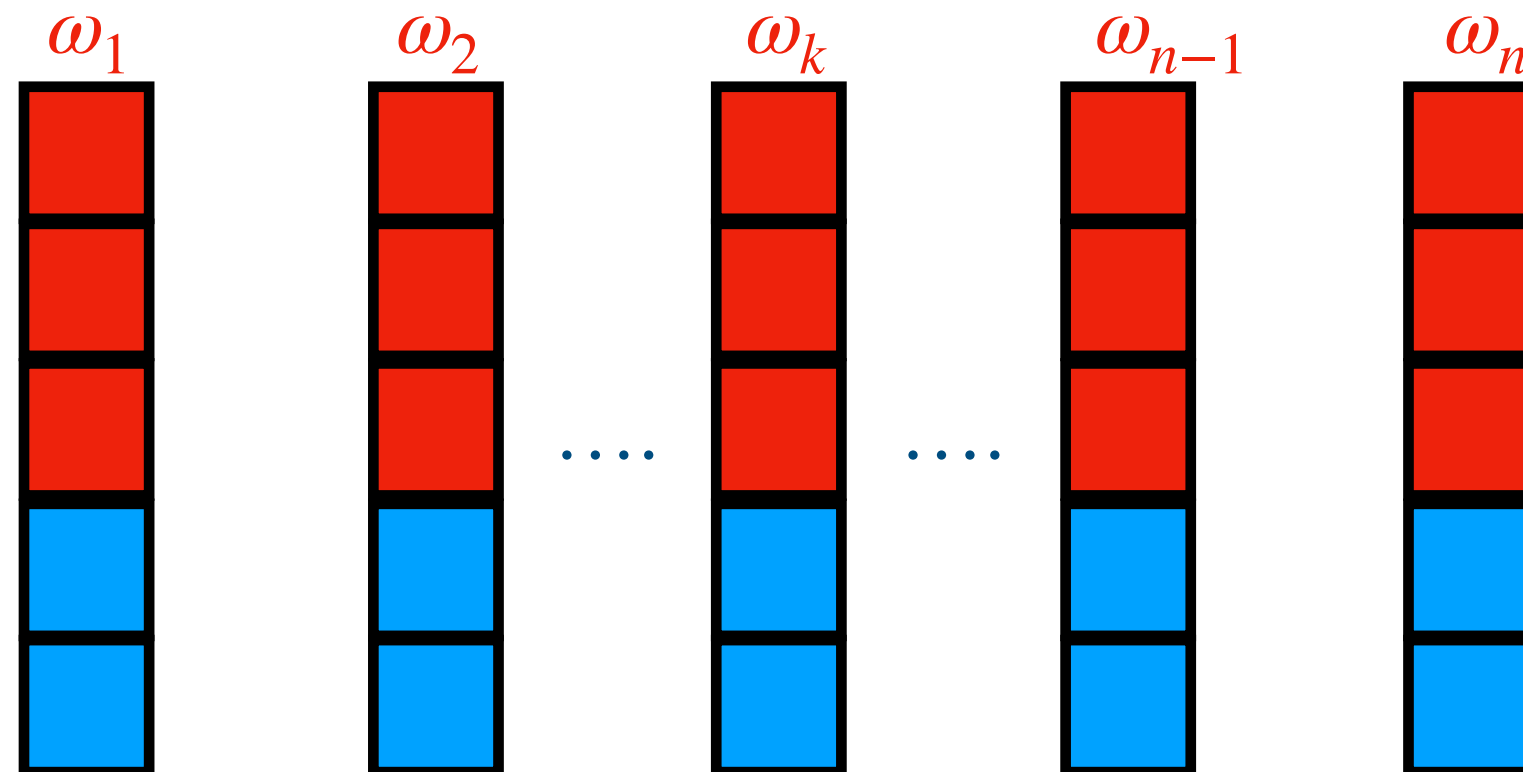
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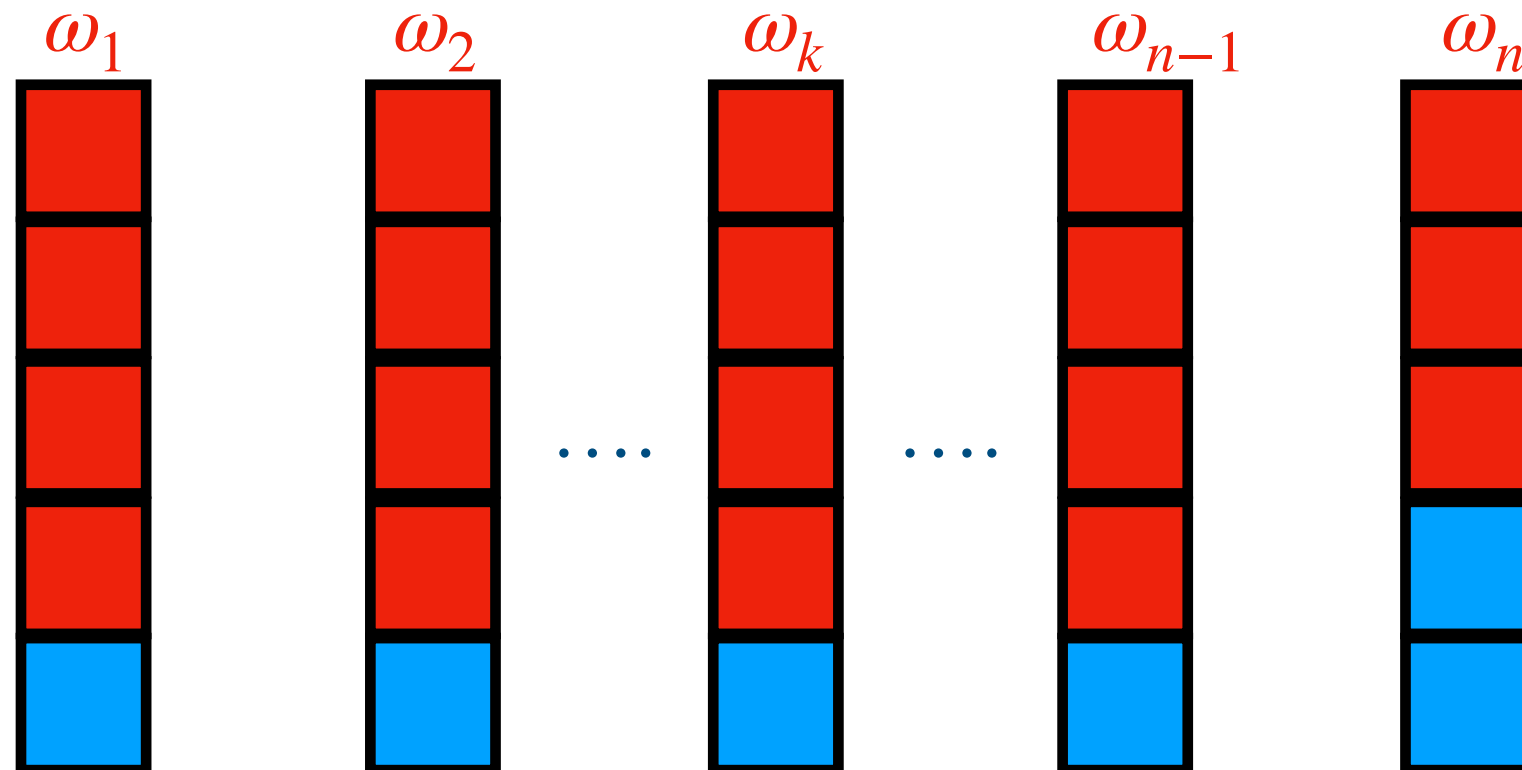
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TMOVE Instantiation

- * Additive Homomorphic Encryption scheme: ElGamal “in the exponent” (homomorphic ElGamal) :

$$Enc_Y(\omega) = \{C_1, C_2\} = \{\omega G + rY, rG\}$$

$$\begin{array}{lcl}
 \text{Additively-Homomorphism:} & (B_1, B_2) = \{\omega G + rY, rG\} & \\
 & + & \\
 & (C_1, C_2) = \{aG + sY, sG\} & \\
 \hline
 & = & (D_1, D_2) = \{(a + \omega)G + (r + s)Y, (r + s)G\}
 \end{array}$$

TMOVE Instantiation

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- * We do the following for party i and PVSS secret α_j :

$$C_1[i, j] = [\omega_i]_j G + \alpha_j pk_i$$

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- * Gradual release: α_j are reconstructed one at a time such that at any given moment the difference between parties is no more than one encrypted segment

Verifiable Social Recovery via TMOVE

Service
Provider



Owner i



Verifiable Social Recovery via TMOVE

Service
Provider

Owner i

2P keyGen

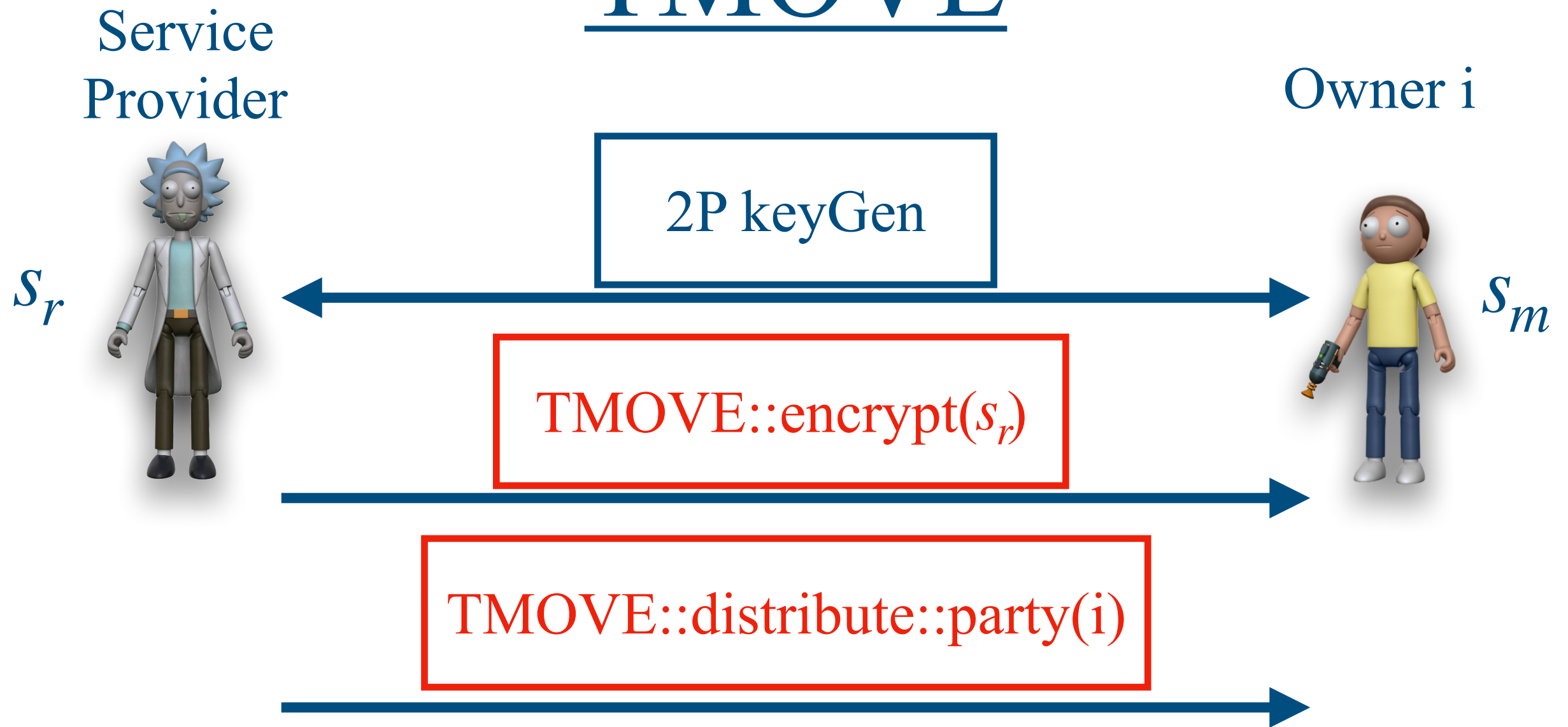
s_r



s_m

$$sk = f(s_r, s_m)$$

Verifiable Social Recovery via TMOVE



Verifiable Social Recovery via TMOVE/ part2



...

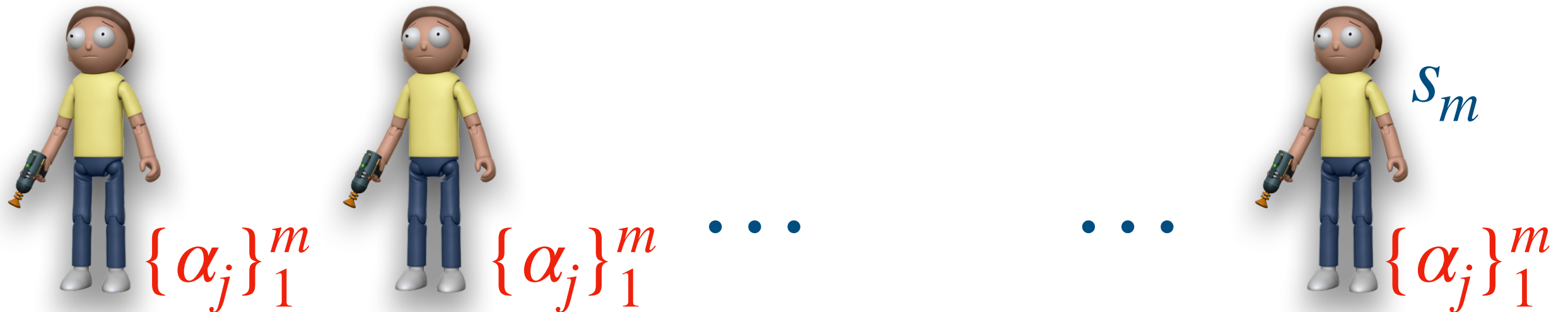
...



S_m

Verifiable Social Recovery via TMOVE/ part2

TMOVE::reconstruct



Verifiable Social Recovery via TMOVE/ part2



TMOVE::decrypt::party(i)

Mixed Model {t=n=2}

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- ▶ Service Providers *x 1*

* System Requirements

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- ▶ *Recovery is possible at all times ?*

Mixed Model {t=n=2}

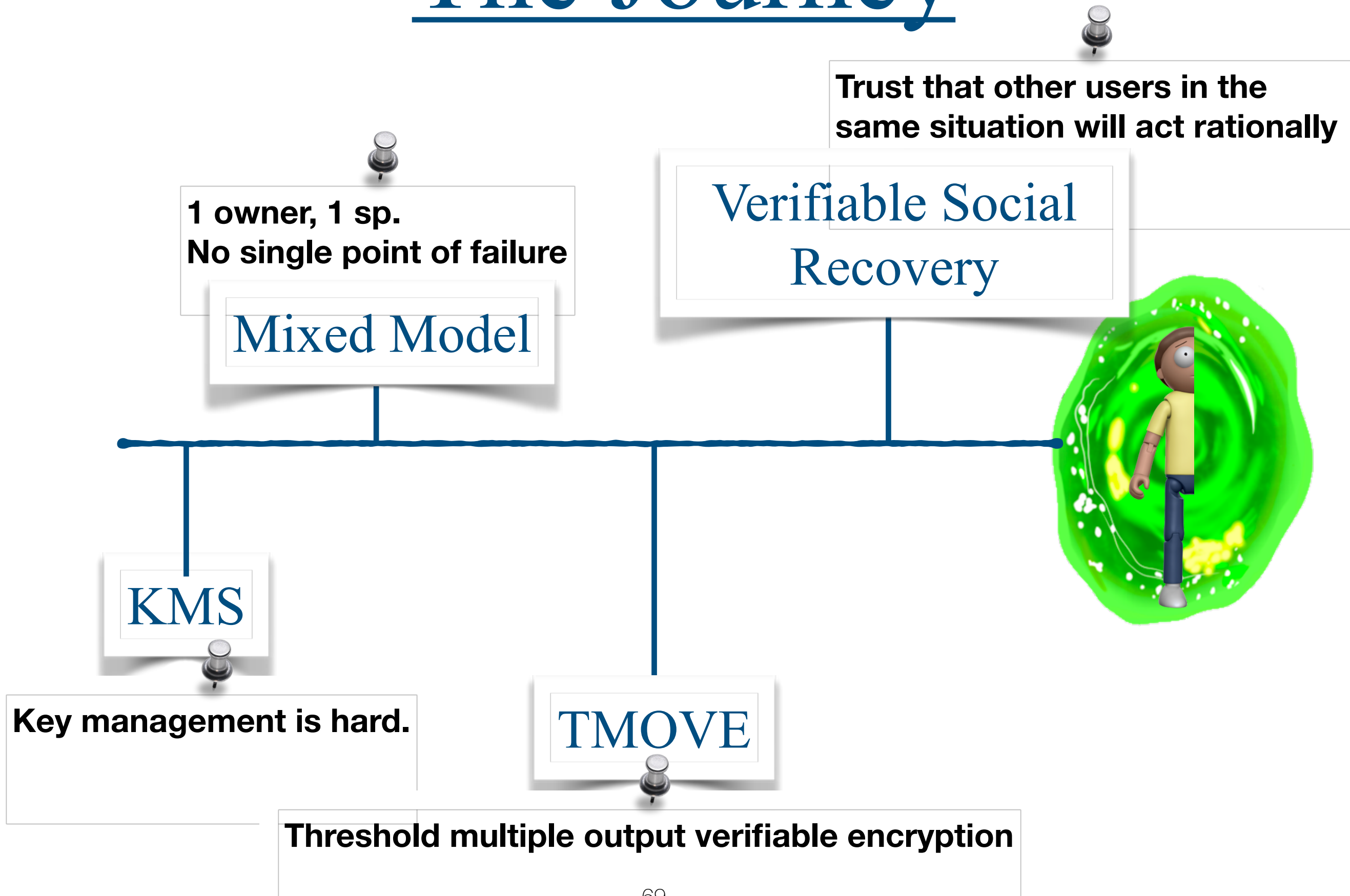
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The Journey





<https://github.com/KZen-networks>

Practical Considerations

- *One SP can handle millions of Owners
- *Owners can join the service Asynchronously
- *Owners of the same SP must have similar stake in the system
- *PKI: Owners of the same SP must know each other public key (blockchain pk's are good)

LET'S JUST SEE WHERE THIS GOES...